

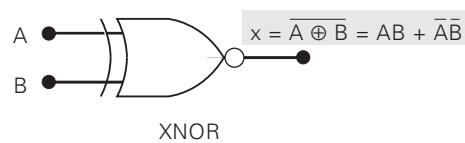
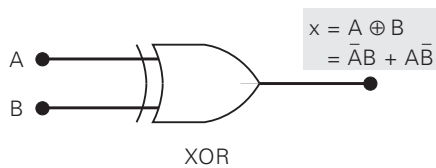
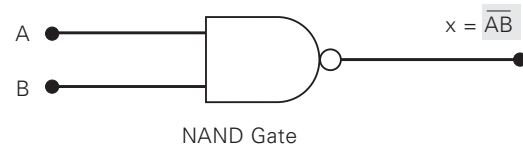
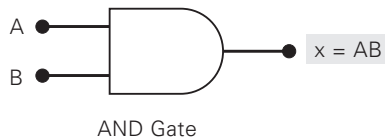
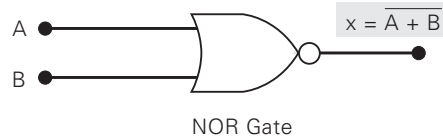
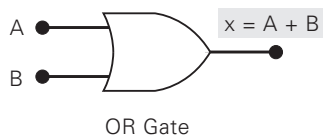
BOOLEAN THEOREMS

- | | | |
|---|---|--|
| 1. $x \cdot 0 = 0$ | 2. $x \cdot 1 = x$ | 3. $x \cdot x = x$ |
| 4. $x \cdot \bar{x} = 0$ | 5. $x + 0 = x$ | 6. $x + 1 = 1$ |
| 7. $x + x = x$ | 8. $x + \bar{x} = 1$ | 9. $x + y = y + x$ |
| 10. $x \cdot y = y \cdot x$ | 11. $x + (y + z) = (x + y) + z = x + y + z$ | 12. $x(yz) = (xy)z = xyz$ |
| 13a. $x(y + z) = xy + xz$ | 13b. $(w + x)(y + z) = wy + xy + wz + xz$ | 14. $x + xy = x$ |
| 15a. $x + \bar{x}y = x + y$ | 15b. $\bar{x} + xy = \bar{x} + y$ | 16. $\overline{x + y} = \bar{x} \bar{y}$ |
| 17. $\overline{xy} = \bar{x} + \bar{y}$ | | |

LOGIC GATE TRUTH TABLES

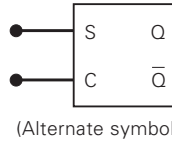
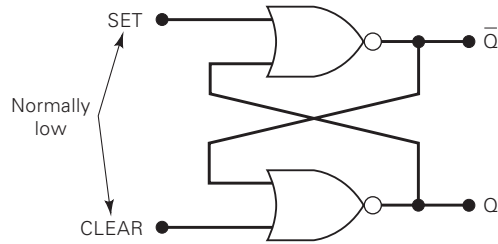
A	B	OR $A + B$	NOR $\overline{A + B}$	AND $A \cdot B$	NAND $\overline{A \cdot B}$	XOR $A \oplus B$	XNOR $\overline{A \oplus B}$
0	0	0	1	0	1	0	1
0	1	1	0	0	1	1	0
1	0	1	0	0	1	1	0
1	1	1	0	1	0	0	1

LOGIC GATE SYMBOLS



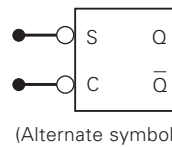
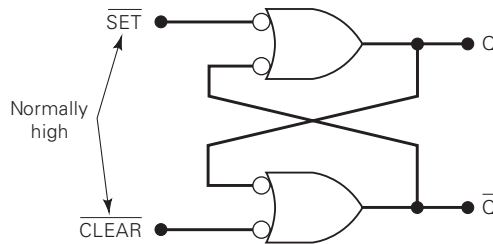
FLIP-FLOPS

NOR Latch



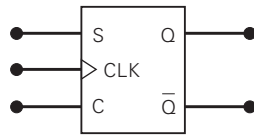
S	C	Q
0	0	No change
1	0	Q = 1
0	1	Q = 0
1	1	Invalid

NAND Latch



S	C	Q
0	0	Invalid
1	0	Q = 0
0	1	Q = 1
1	1	No change

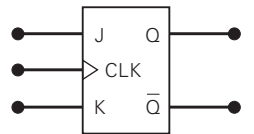
Clocked S-C



S	C	CLK	Q
0	0	↑	Q ₀ (no change)
1	0	↑	1
0	1	↑	0
1	1	↑	Ambiguous

↓ of CLK has no effect on Q

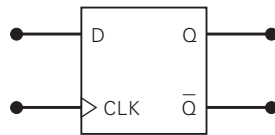
Clocked J-K



J	K	CLK	Q
0	0	↑	Q ₀ (no change)
1	0	↑	1
0	1	↑	0
1	1	↑	Q ₀ (toggles)

↓ of CLK has no effect on Q

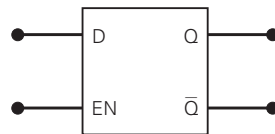
Clocked D



D	CLK	Q
0	↑	0
1	↑	1

↓ of CLK has no effect on Q

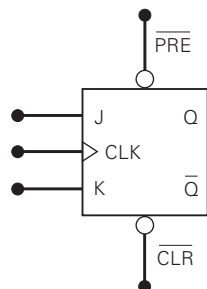
D Latch



EN	D	Q*
0	X	No change
1	0	0
1	1	1

*Q follows D input while EN is HIGH

Asynchronous Inputs



PRE-bar	CLR-bar	Q*
1	1	No effect; FF can respond to J, K and CLK
1	0	Q = 0 independent of J, K, CLK
0	1	Q = 1 independent of J, K, CLK
0	0	Ambiguous (not used)

*CLK can be in any state