

Figure 3.13 Simple solar cell structure used to analyze the operation of a solar cell. Free carriers have diffused across the junction (x = 0) leaving a space-charge or depletion region practically devoid of any free or mobile charges. The fixed charges in the depletion region are due to ionized donors on the *n*-side and ionized acceptors on the *p*-side

where  $\phi$  is the electrostatic potential, q is magnitude of the electron charge,  $\varepsilon$  is the electric permittivity of the semiconductor,  $p_o$  is the equilibrium hole concentration,  $n_o$  is the equilibrium electron concentration,  $N_A^-$  is the ionized acceptor concentration, and  $N_D^+$  is the ionized donor concentration. Equation 3.82 is a restatement of equation 3.70 for the given conditions.

This equation is easily solved numerically; however, an approximate analytic solution for an abrupt *pn*-junction can be obtained that lends physical insight into the formation of the space-charge region. Figure 3.13 depicts a simple one-dimensional (1D) *pn*-junction solar cell (diode), with the metallurgical junction at x = 0, which is uniformly doped  $N_D$ on the *n*-type side and  $N_A$  on the *p*-type side. For simplicity, it is assumed that the each side is nondegenerately doped and that the dopants are fully ionized.

Within the depletion region, defined by  $-x_N < x < x_P$ , it can be assumed that  $p_o$  and  $n_o$  are both negligible compared to  $|N_A - N_D|$  so that equation (3.82) can be simplified to

$$\nabla^2 \phi = -\frac{q}{\varepsilon} N_{\rm D}, \quad \text{for} - x_N < x < 0 \quad \text{and}$$
  

$$\nabla^2 \phi = \frac{q}{\varepsilon} N_{\rm A}, \quad \text{for} \quad 0 < x < x_P$$
(3.83)

Outside the depletion region, charge neutrality is assumed and

$$\nabla^2 \phi = 0 \quad \text{for} \quad x \le -x_N \quad \text{and} \quad x \ge x_P.$$
 (3.84)

This is commonly referred to as the *depletion approximation*. The regions on either side of the depletion regions are the quasi-neutral regions.

The electrostatic potential difference across the junction is the built-in voltage,  $V_{bi}$ , and can be obtained by integrating the electric field,  $\vec{E} = -\nabla\phi$ .

$$\int_{-x_N}^{x_P} \vec{E} dx = -\int_{-x_N}^{x_P} \frac{d\phi}{dx} dx = -\int_{V(-x_N)}^{V(x_P)} d\phi = \phi(-x_N) - \phi(x_P) = V_{\text{bi}}$$
(3.85)