

Figure 11.23 Cross section of a parabolic reflective concentrator

Now consider a ray that arrives at a small angle θ_{in} to the normal axis. It can be calculated that it will intercept the receiver at a distance *s* from the focus given by

$$s = \frac{r\sin\theta_{\rm in}}{\cos\theta_r} = \frac{2F\sin\theta_{\rm in}}{\cos\theta_r(1+\cos\theta_r)}$$

This shows that s increases as one moves toward the rim, increasing θ_r . Clearly, the rays hitting the rim at x = D/2 will have the largest s. Noting that the total receiver size, S, required to capture all rays up to incident angles of $\pm \theta_{\text{max,in}}$ is $S = 2s_{\text{max}}$, gives

$$S = \frac{4F\sin\theta_{\max,\text{in}}}{\cos\theta_{\max,r}(1+\cos\theta_{\max,r})} = D\frac{\sin\theta_{\max,\text{in}}}{\cos\theta_{\max,r}\sin\theta_{\max,r}}$$

For a two-dimensional parabolic trough, the concentration ratio is C = D/S, giving

$$C = \cos \theta_{\max,r} \frac{\sin \theta_{\max,r}}{\sin \theta_{\max,in}}$$

It is interesting to note that the maximum concentration for a parabola without a secondary occurs at a rim angle of 45° (which corresponds to an *f*-number of 0.6) and is

$$C = \frac{1}{2} \frac{1}{\sin \theta_{\max, in}}$$

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